Quantum science needs mathematicians

Bert de Jong Director Quantum Systems Accelerator Director MACH-Q Program

wadejong@lbl.gov

Quantum is already used in every day life

MRI

Lighting

GPS with atomic clocks

Optical fibers in telecom

Lasers

Ubiquitous transistors

Ingredients that make quantum *quantum*

 $-2 -$

Superpostion and Schrödinger's Cat

- \Box You can only MEASURE either dead or alive, not both
- \Box How you measure (which basis) determines if you get information or gibberish

Einstein did not like this uncertainty

"I, at any rate, am convinced that He [God] does not throw dice."

~Albert Einstein on Quantum Mechanics "Einstein, stop telling God what to do."

~Niels Bohr on Einstein's feeling about Quantum Physics

Niels Bohr's office in Copenhagen

Two-slit experiment proved superposition and uncertainty

WAVE-PARTICLE WEIRDNESS

When quantum objects such as electrons are fired one by one through a pair of closely spaced slits, they behave like particles: each one hits a screen placed on the far side at exactly one point. But they also behave like waves: successive hits build up a banded interference pattern exactly like that generated by a wave passing through the slits (bottom). This wave-particle duality is described by a mathematical tool known as the wavefunction.

Even large proteins show quantum behavior

Credit: Yaakov Fein Universität Wien

onature

- 5 -

Entanglement is what makes quantum powerful

- 6 -

Measuring a Pair of Entangled Photons if 1 is then 2 must red be blue

aaaa **BERKELEY LAI**

$\overline{2}$ then 2 must if 1 is blue be red $\overline{2}$

EINSTEIN ATTACKS QUANTUM THEORY

Scientist and Two Colleagues Find It Is Not 'Complete' Even Though 'Correct.'

SEE FULLER ONE POSSIBLE

Believe a Whole Description of 'the Physical Reality' Can Be Provided Eventually.

Einstein called it "spooky action at a distance"

Entanglement and quantum correlations

Quantum information can be stored *nonlocal*

and is stored in *quantum correlations* between qubits

Based on Preskill (CalTech) Wolfgang Pauli Lecture 2024

Entanglement and quantum correlations

Classically of a whole collective measurement, possible knowledge of all its a *Not so with quantum information in a quantum book* (reading of all pages in quantum book at the same time) \bm{t} eals $\bm{\nu}$ the \bm{q} nformaatio \bm{q} formationed in the aquiloms:

Based on Preskill (CalTech) Wolfgang Pauli Lecture 2024

Twentieth century quantum revolution

Quantum computing Next-level simulations

Quantum networks Secure data communication

Quantum sensors From materials to gravitational waves

Credit: Georgia Mansell/LIGO Hanford

Simulating evolution of a quantum system on a classical computer in an efficient way is impossible (Feynman, 1982)

Shor developed factorization algorithm with quantum advantage

Logarithms on a Quantum Computer

Author: Peter W. Shor | AUTHORS INFO & AFFILIATIONS

https://doi.org/10.1137/S0097539795293172

SIAM J. Sci. Statist. Comput. 26 (1997) 1484

Information content of quantum computers is key

• 2ⁿ complex coefficients describe the state of a composite quantum system with n qubits

• 100 qubits = 2^{100} states

• Quickly reaches number of particles in the universe

Accelerating DOE discovery science with quantum computing

Algorithmic speedups over classical computing

Quantum simulation

Efficient optimization algorithms

"Unbreakable" encryption protocols

Quantum computing advantage for molecular sciences

Nature's answer to Haber Process

Single energy calculation is inaccessible, even at exascale! Quantum computer requires ~100-200 ideal qubits for solution

Electron correlation drives many materials technologies

Superconductivity in MRI magnets and wires for current transmission

Strongly correlated materials in battery materials

Accurate solutions are challenging to impossible on classical computers

Quantum advantage exploring fundamental laws of physics

Image inspired by JHEP 02 (2009) 007, Courtesy Nachman (LBNL)

Image from arXiv:2101.05821

Quantum Simulation for High Energy Physics

Christian W. Bauer, ^{1, a} Zohreh Davoudi, ^{2, b} A. Baha Balantekin, ³ Tanmoy Bhattacharya, ⁴ Marcela Carena, 5, 6, 7, 8 Wibe A. de Jong, ¹ Patrick Draper, ⁹ Aida El-Khadra, ⁹ Nate Gemelke.¹⁰ Masanori Hanada.¹¹ Dmitri Kharzeev.^{12, 13} Henry Lamm.⁵ Ying-Ying Li,⁵ Junyu Liu,^{14,15} Mikhail Lukin,¹⁶ Yannick Meurice,¹⁷ Christopher Monroe, ^{18, 19, 20, 21} Benjamin Nachman,¹ Guido Pagano,²² John Preskill,²³ Enrico Rinaldi, 24, 25, 26 Alessandro Roggero, 27, 28 David I. Santiago, 29, 30 Martin J. Savage, 31 Irfan Siddiqi, 29, 30, 32 George Siopsis, 33 David Van Zanten, 5 Nathan Wiebe, 34, 35 Yukari Yamauchi, 2 Kübra Yeter-Aydeniz, 36 and Silvia Zorzetti⁵

PRX Quantum **4**, 027001 (2023) *arXiv:2105.13849*

Quantum Computing for Inflationary, Dark Energy and Dark matter Cosmology

Amy Joseph¹, Juan-Pablo Varela², Molly P. Watts³, Tristen White⁴, Yuan Feng⁵, Mohammad Hassan⁶, Michael McGuigan⁷,

Speedup not only factor for quantum advantage

Power: 20 MW + 10 MW for cooling **Cost:** US\$600M (estimated cost) **Space:** 2225 m² (7,300 sq ft) 24,000 house holds

Quantum computers could solve **larger problems faster** compared to classical computing hardware

Quantum computers potentially **cheaper and use less energy** than classical computers, increasing accessibility to large scale computing

Quantum computers come in many flavors

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Quantum systems are getting higher gate fidelities

PHYSICAL REVIEW LETTERS

Different technologies achieve 99.9% fidelity on 2-qubit entangling gates

Quantinuum extends its significant lead in quantum computing, achieving historic milestones for hardware **fidelity and Quantum Volume**

Quantinuum has raised the bar for the global ecosystem by achieving the historic and much-vaunted "three 9's" 2-qubit gate fidelity in its commercial quantum computer and announcing that its Quantum

ssed one million - exponentially higher than its

IQM Quantum Computers achieves new technology milestones with 99.9% 2-qubit gate fidelity and 1 millisecond coherence time

15/07/2024 **8** min. read

• Qubit relaxation time of T1= 0.964 + - 0.092 milliseconds and dephasing time T2 echo 1.155 +- 0.188 milliseconds.

• Two-qubit gates with a record fidelity reaching 99.9%

• The results demonstrate that IQM's in-house chip fabrication has reached quality on par with other world-leading institutions.

Quantum systems get new operation capabilities

High-fidelity qutrit entangling gates for superconducting circuits

Noah Goss^[O], Alexis Morvan, Brian Marinelli, Bradley K. Mitchell, Long B. Nguyen, Ravi K. Naik, Larry Chen, Christian Jünger, John Mark Kreikebaum, David I. Santiago, Joel J. Wallman & Irfan Siddigi

Nature Communications 13, Article number: 7481 (2022) Cite this article

9449 Accesses 48 Altmetric Metrics

Number of qubits in quantum systems is growing

Q QUANTINUUM Products & Solutions Research Company Newc

Quantinuum Launches Industry-First, Trapped-Ion 56-Qubit Quantum Computer, Breaking Key Benchmark Record

IBM also unveiled IBM Quantum System Two, the company's first modular quantum computer and cornerstone of IBM's quantum-centric supercomputing architecture. The first IBM Quantum System Two, located in Yorktown Heights, New York, has begun operations with three IBM Heron processors and supporting control electronics

Quantum startup Atom Computing first to exceed 1,000 **aubits** October 24, 2023

Systems to be available in 2024, on path to fault-tolerant quantum computing this decade

October 24, 2023 - Boulder, CO - Atom Computing announced it has created a 1.225-site atomic array, currently populated with 1,180 qubits, in its next-generation quantum computing platform.

Challenging our ability to simulate and validate

Sprawling quantum industry with great job opportunities

Quantum Systems Accelerator is solving big challenges with integrated teams

QSA integrates researchers with complementary skills from six institutions to create useful quantum systems based on neutral atoms

Challenges to achieving useful quantum computers

Almost enough good qubits for specialized quantum use

Coherence - available compute time - very short (10s-100s of ops), driven by noise and errors

Advances in algorithms, software tools and compilers are needed to make quantum computing broadly approachable

Designing better qubits is hard

Moving towards quantum advantage for science

Hardware technology Scientific algorithms and software

- Increasing lifetimes
- Increasing fidelity and reducing errors
- Reducing qubit count
- Decreasing operation counts
- Incorporating error resiliency

Mathematics is needed everywhere!!!

Applied mathematics critical across the quantum stack

Developing **Novel** Algorithms and Software to Advance **Science with** Quantum

Programming **Tools and Control Protocols to** Harness the Power of Quantum **Computers**

Designing and **Building** Prototype Quantum Processors, Controls, and **Sensors**

Building Prototype Quantum **Network and** Quantum Computing **Testbeds**

Designing chips and control systems with AMR and electromagnetics solvers

Image of ENCHILADA ion trap

Manuscript on arXiv:2403.00208 (2024)

Optimization challenges are everywhere

$$
H = \sum_{i\alpha} g_i^{\alpha} \langle \sigma_{\alpha}^{i} \rangle + \frac{1}{2} \sum_{ij\alpha\beta} g_{ij}^{\alpha\beta} \langle \sigma_{\alpha}^{i} \sigma_{\beta}^{j} \rangle + \cdots
$$

Only prepare and measure, do the rest classically

Home / Proceedings / QCE / QCE 2022

2022 IEEE International Conference on Quantum Computing and Engineering (QCE)

Accelerating Noisy VQE Optimization with Gaussian **Processes**

Year: 2022, Pages: 215-225 DOI Bookmark: 10.1109/QCE53715.2022.00041

Authors

Juliane Muller, Lawrence Berkeley National Laboratory, Computing Sciences Area, Berkeley, CA, USA Wim Lavrijsen, Lawrence Berkeley National Laboratory, Computing Sciences Area, Berkeley, CA, USA Costin lancu, Lawrence Berkeley National Laboratory, Computing Sciences Area, Berkeley, CA, USA Wibe de Jong, Lawrence Berkeley National Laboratory.Computing Sciences Area, Berkeley, CA, USA

- 28 - https://scikit-quant.readthedocs.io

Compiling…General Synthesis Problem

Unitary **Circuit**

Quantum Compilation: *Given unitary U, find decomposition in terms of gates G from a (universal) fixed gate set*

Enables:

- Algorithm discovery
- Gate set and hardware exploration
- Global circuit optimization

Many opportunities to improve noisy optimization

Chadwick, Chong, QCE23, doi:10.1109/QCE57702.2023.00145

Quantum algorithms rely on applied mathematics

Special care needs to be taken in general eigensolver due to noise in data!

 $HC = SCE$

- 31 - Urbanek, Van Beeumen, et al., J. Chem. Theory Comput. 16, 5425 (2020)

FABLE: Fast Approximate BLock-Encodings

Circuit synthesis tool for block encoded operators

Block encoding:

…

$$
U = \begin{bmatrix} A & * \\ * & * \end{bmatrix}
$$

- **• Non-unitary** evolution on a quantum computer: Quantum linear systems, dynamic simulation, ground states, quantum thermodynamics, open quantum systems,
- FABLE circuits are:

easy to generate directly in CX, Ry and H gates efficiently **compressible**

Gate complexities for 1D and 2D Laplacian

Camps, Van Beeumen, QCE22 - DOI:10.1109/QCE53715.2022.00029

Building on Quantum Subspace Expansion: Real-time evolution for eigenvalue extraction

 \sim **BERKELEY LAI**

Real time evolution to generate a basis of expansion states: $|\Phi_{j,0}\rangle=e^{-iHt_j}|\Psi_0\rangle$

$$
\begin{array}{llll}\n\hspace{0.5cm} & \text{\rm if } \ \Psi_0 \rangle & \qquad \qquad |\Phi_{1,0} \rangle & \qquad |\Phi_{2,0} \rangle & \qquad |\Phi_{3,0} \rangle & \qquad |\Phi_{N,0} \rangle \\
\text{Initial vector} & & & \\\text{\rm Use as a basis to solve:} & \qquad H \Psi = E S \Psi & S_{i,j} = \langle \Phi_i | H | \Phi_j \rangle & \qquad \qquad \\\end{array}
$$

Possible to extract eigenstates by the cancellation of phases of components of the initial vector.

Promising because unlike imaginary, real time evolution is native to quantum computing.

- 33 - *Klymko, de Jong, Tubman et al., PRX Quantum 3 (2022)*

Building on quantum subspace expansion to extract excited states: Variational Quantum Phase Estimation (VQPE)

Original generalized eigenvalue equation:

Unitary form:

$$
H\mathbf{c} = ES\mathbf{c}
$$
\n
$$
U(\Delta t)_{j,k} = \langle \Psi_0 | e^{-iH(\Delta t + t_k - t_j)} | \Psi_0 \rangle = S_{j,k+1} = S_{j-1,k}
$$

Autocorrelation Function

Toeplitz structure!

Toeplitz structure means that we only need a *linear* number of measurements instead of quadratic

Approach allows extraction of the maximal number of excited states!

 \cdot π Λ μ

- 34 - *Klymko, de Jong, Tubman et al., PRX Quantum 3 (2022)*

Noise in quantum systems is the biggest nemesis

Any interaction between the qubits and their environment leads to information loss

Useful quantum science through error correction

Encode the information in multiple qubits with *nonlocal* correlations

New error correction codes are being developed

Bravyi et al., npj Quant. Inf. 4, 55 (2018) Chamberland et al., Phys. Rev. X 10, 011022 (2020)

Full error correction (hardware or software) a long-term solution, driven by increases in qubit counts and increases in fidelity

Simple error detection and mitigation works

2 logical qubit H2 molecule on 6 qubits with minimal basis

Urbanek et al, Phys. Rev. A 102, 022427 (2020)

First demonstrations of error correction in 2024

Demonstration of quantum computation and error correction with a tesseract code

Ben W. Reichardt,¹ David Aasen,¹ Rui Chao,¹ Alex Chernoguzov,² Wim van Dam,¹ John P. Gaebler,² Dan Gresh.² Dominic Lucchetti.² Michael Mills.² Steven A. Moses.² Brian Nevenhuis.² Adam Paetznick.¹ Andres Paz,¹ Peter E. Siegfried,² Marcus P. da Silva,¹ Krysta M. Svore,¹ Zhenghan Wang,¹ and Matt Zanner¹

1 Microsoft Azure Quantum 2 *Ouantinuum*

A critical milestone for quantum computers is to demonstrate fault-tolerant computation that outperforms computation on physical qubits. The tesseract subsystem color code protects four logical qubits in 16 physical qubits, to distance four. Using the tesseract code on Quantinuum's trapped-ion quantum computers, we prepare high-fidelity encoded graph states on up to 12 logical qubits, beneficially combining for the first time fault-tolerant error correction and computation. We also protect encoded states through up to five rounds of error correction. Using performant quantum software and hardware together allows moderate-depth logical quantum circuits to have an order of magnitude less error than the equivalent unencoded circuits.

Article | Open access | Published: 27 March 2024

High-threshold and low-overhead fault-tolerant quantum memory

Sergey Bravyi, Andrew W. Cross, Jay M. Gambetta, Dmitri Maslov ⊠, Patrick Rall & Theodore J. Yoder

Nature 627, 778-782 (2024) | Cite this article

36k Accesses | 31 Citations | 342 Altmetric | Metrics

Abstract

The accumulation of physical errors^{1,2,3} prevents the execution of large-scale algorithms in current quantum computers. Quantum error correction⁴ promises a solution by encoding k logical qubits onto a larger number n of physical qubits, such that the physical errors are suppressed enough to allow running a desired computation with tolerable fidelity. Quantum error correction becomes practically realizable once the physical error rate is below a threshold value that depends on the choice of quantum code, syndrome measurement circuit and decoding algorithm⁵. We present an end-to-end quantum error correction protocol that implements fault-tolerant memory on the basis of a family of low-density parity-check codes⁶. Our approach achieves an error threshold of 0.7% for the standard circuit-based noise Article Open access Published: 06 December 2023

Logical quantum processor based on reconfigurable atom arrays

Doley Bluystein, Simon J. Evered, Alexandra A. Geim, Sophie H. Li, Hengyun Zhou, Tom Manovitz, Sepehr Ebadi, Madelyn Cain, Marcin Kalinowski, Dominik Hangleiter, J. Pablo Bonilla Ataides, Nishad Maskara, Iris Cong, Xun Gao, Pedro Sales Rodriguez, Thomas Karolyshyn, Giulia Semeghini, Michael J. Gullans, Markus Greiner, Vladan Vuletić & Mikhail D. Lukin[∞]

Nature 626, 58-65 (2024) | Cite this article

121k Accesses | 122 Citations | 958 Altmetric | Metrics

Quantum error correction below the surface code threshold

Google Quantum AI and Collaborators (Dated: August 27, 2024)

Quantum error correction $[1-4]$ provides a path to reach practical quantum computing by combining multiple physical qubits into a logical qubit, where the logical error rate is suppressed exponentially as more qubits are added. However, this exponential suppression only occurs if the physical error rate is below a critical threshold. In this work, we present two surface code memories operating below this threshold: a distance-7 code and a distance-5 code integrated with a real-time decoder. The logical error rate of our larger quantum memory is suppressed by a factor of $\Lambda = 2.14 \pm 0.02$ when increasing the code distance by two, culminating in a 101-qubit distance-7 code with 0.143% \pm 0.003% error per cycle of error correction. This logical memory is also beyond break-even, exceeding its best physical qubit's lifetime by a factor of 2.4 ± 0.3 . We maintain below-threshold performance when decoding in real time, achieving an average decoder latency of 63 us at distance-5 up to a million cycles, with a cycle time of 1.1 us. To probe the limits of our error-correction performance, we run repetition codes up to distance-29 and find that logical performance is limited by rare correlated error events occurring approximately once every hour, or 3×10^9 cycles. Our results present device performance that, if scaled, could realize the operational requirements of large scale fault-tolerant quantum algorithms.

Understanding quantum computers through validation

Approach enables verification, by efficiently quantifying how accurately a given computer can implement a given algorithm's quantum circuits

Uses three classes of "mirror circuits" whose success rates can be efficiently measured

Proctor et al., arXiv:2204.07568 -40

Solving problems beyond the reach of current hardware

CutQC: Using Small Quantum Computers for Large Quantum Circuit Evaluations

ASPLOS 21 - arXiv:2012.02333

Divide-and-conquer, where the cost of stitching the problem back together depends on sparsity

Race to the moon delivered many ancillary technologies

Quantum-inspired algorithms speedup classical computing

Novel quantum hardware technologies find way into classical computing hardware

Better understanding of quantum physics to lead to advances in classical computing

CMOS sensor, using integrated circuits….

Race for a universal quantum computer is already showing impacts beyond quantum computing

I hope I convinced you that…

Quantum is not scary

And math is important for quantum

Bert de Jong wadejong@lbl.gov

