# Quantum science needs mathematicians

# Bert de Jong Director Quantum Systems Accelerator Director MACH-Q Program



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## Quantum is already used in every day life



MRI



Lighting



GPS with atomic clocks



Optical fibers in telecom



Lasers



Ubiquitous transistors



### Ingredients that make quantum quantum



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## Superpostion and Schrödinger's Cat



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- You can only MEASURE either dead or alive, not both
- How you measure (which basis) determines if you get information or gibberish



## Einstein did not like this uncertainty

"I, at any rate, am convinced that He [God] does not throw dice."

~Albert Einstein on Quantum Mechanics "Einstein, stop telling God what to do."

~Niels Bohr on Einstein's feeling about Quantum Physics



Niels Bohr's office in Copenhagen



### Two-slit experiment proved superposition and uncertainty

### WAVE-PARTICLE WEIRDNESS

When quantum objects such as electrons are fired one by one through a pair of closely spaced slits, they behave like particles: each one hits a screen placed on the far side at exactly one point. But they also behave like waves: successive hits build up a banded interference pattern exactly like that generated by a wave passing through the slits (bottom). This wave-particle duality is described by a mathematical tool known as the wavefunction.



### Even large proteins show quantum behavior



Credit: Yaakov Fein Universität Wien



©nature

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## Entanglement is what makes quantum powerful

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Measuring a Pair of Entangled Photons if 1 is then 2 must red be blue



mm

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### EINSTEIN ATTACKS QUANTUM THEORY

Scientist and Two Colleagues Find It Is Not 'Complete' Even Though 'Correct.'

### SEE FULLER ONE POSSIBLE

Believe a Whole Description of 'the Physical Reality' Can Be Provided Eventually.



Einstein called it "spooky action at a distance"

## **Entanglement and quantum correlations**



### Quantum information can be stored *nonlocal*

### and is stored in quantum correlations between qubits

Based on Preskill (CalTech) Wolfgang Pauli Lecture 2024

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### **Entanglement and quantum correlations**



Classically of a whole does not necessarily include the best possible knowledge of all its parts, (reading of all pages in quantum book at the same time) Net/eals/the proceedings of the Cambridge Philosophical Society

Based on Preskill (CalTech) Wolfgang Pauli Lecture 2024



## Twentieth century quantum revolution

Quantum computing Next-level simulations



Quantum networks Secure data communication



Quantum sensors From materials to gravitational waves



Credit: Georgia Mansell/LIGO Hanford



# Simulating evolution of a quantum system on a classical computer in an efficient way is impossible (Feynman, 1982)







### Shor developed factorization algorithm with quantum advantage



Author: Peter W. Shor <u>AUTHORS INFO & AFFILIATIONS</u>

https://doi.org/10.1137/S0097539795293172

### SIAM J. Sci. Statist. Comput. 26 (1997) 1484





# Information content of quantum computers is key

2<sup>n</sup> complex coefficients describe the state of a composite quantum system with n qubits

• 100 qubits =  $2^{100}$  states



• Quickly reaches number of particles in the universe



### Accelerating DOE discovery science with quantum computing

### **Algorithmic speedups over classical computing**

### **Quantum simulation**

### **Efficient optimization algorithms**

### "Unbreakable" encryption protocols











### Quantum computing advantage for molecular sciences



### Nature's answer to Haber Process

### Single energy calculation is inaccessible, even at exascale! Quantum computer requires ~100-200 ideal qubits for solution



### **Electron correlation drives many materials technologies**



Superconductivity in MRI magnets and wires for current transmission

Strongly correlated materials in battery materials

### Accurate solutions are challenging to impossible on classical computers





### Quantum advantage exploring fundamental laws of physics



Image inspired by JHEP 02 (2009) 007, Courtesy Nachman (LBNL)







Image from arXiv:2101.05821

#### Quantum Simulation for High Energy Physics

Christian W. Bauer,<sup>1, a</sup> Zohreh Davoudi,<sup>2, b</sup> A. Baha Balantekin,<sup>3</sup> Tanmoy Bhattacharya,<sup>4</sup>
Marcela Carena,<sup>5, 6, 7, 8</sup> Wibe A. de Jong,<sup>1</sup> Patrick Draper,<sup>9</sup> Aida El-Khadra,<sup>9</sup>
Nate Gemelke,<sup>10</sup> Masanori Hanada,<sup>11</sup> Dmitri Kharzeev,<sup>12, 13</sup> Henry Lamm,<sup>5</sup>
Ying-Ying Li,<sup>5</sup> Junyu Liu,<sup>14, 15</sup> Mikhail Lukin,<sup>16</sup> Yannick Meurice,<sup>17</sup>
Christopher Monroe,<sup>18, 19, 20, 21</sup> Benjamin Nachman,<sup>1</sup> Guido Pagano,<sup>22</sup> John Preskill,<sup>23</sup>
Enrico Rinaldi,<sup>24, 25, 26</sup> Alessandro Roggero,<sup>27, 28</sup> David I. Santiago,<sup>29, 30</sup>
Martin J. Savage,<sup>31</sup> Irfan Siddiqi,<sup>29, 30, 32</sup> George Siopsis,<sup>33</sup> David Van Zanten,<sup>5</sup>
Nathan Wiebe,<sup>34, 35</sup> Yukari Yamauchi,<sup>2</sup> Kübra Yeter-Aydeniz,<sup>36</sup> and Silvia Zorzetti<sup>5</sup>

### PRX Quantum 4, 027001 (2023)

Quantum Computing for Inflationary, Dark Energy and Dark matter Cosmology

Amy Joseph<sup>1</sup>, Juan-Pablo Varela<sup>2</sup>, Molly P. Watts<sup>3</sup>, Tristen White<sup>4</sup>, Yuan Feng<sup>5</sup>, Mohammad Hassan<sup>6</sup>, Michael McGuigan<sup>7</sup>,

### arXiv:2105.13849



### Speedup not only factor for quantum advantage



**Power: 2**0 MW + 10 MW for cooling **Cost:** US\$600M (estimated cost) **Space:** 2225 m<sup>2</sup> (7,300 sq ft) 24,000 house holds

Quantum computers could solve <u>larger problems faster</u> compared to classical computing hardware

Quantum computers potentially <u>cheaper and use less energy</u> than classical computers, increasing accessibility to large scale computing



## Quantum computers come in many flavors



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# Quantum systems are getting higher gate fidelities

PHYSICAL REVIEW LETTERS

# Different technologies achieve 99.9% fidelity on 2-qubit entangling gates

Quantinuum extends its significant lead in quantum computing, achieving historic milestones for hardware fidelity and Quantum Volume

Quantinuum has raised the bar for the global ecosystem by achieving the historic and much-vaunted "three 9's" 2-qubit gate fidelity in its commercial quantum computer and announcing that its Quantum

ssed one million – exponentially higher than its ors.

IQM Quantum Computers achieves new technology milestones with 99.9% 2-qubit gate fidelity and 1 millisecond coherence time

15/07/2024 🕒 8 min. read

Qubit relaxation time of T1= 0.964 +- 0.092 milliseconds and dephasing time T2 echo 1.155
+- 0.188 milliseconds.

Two-qubit gates with a record fidelity reaching 99.9%

• The results demonstrate that IQM's in-house chip fabrication has reached quality on par with other world-leading institutions.

	Desert			A	Deference	Coorob	Draga	Jrs.
nights	Recent	Accepted	Collections	Authors	Referees	Search	Press	Article Open access Published: 11 October 2023
							Acc	High-fidelity parallel entangling gates on a neutral-
High- Super	Fidelity, rconduc	High-So ting Qui	alability <sup>-</sup> bits	Two-Qub	oit Gate	Schem	atom quantum computer	
uan Xu,	Ji Chu, Jiaha	o Yuan, Jiawe	ei Qiu, Yuxuan I	Zhou, Libo Zh	ang, Xinsher	ng Tan, Yang	Yu, Son	Simon J. Evered, Dolev Bluvstein, Marcin Kalinowski, Sepehr Ebadi, Tom Manovitz, Hengyun Zhou,
hys. Rev. Lett. <b>125</b> , 240503 – Published 9 December 2020								Sopnie H, Li, Alexandra A, Geim, Tout T, Wang, Nishad Maskara, Harry Levine, Giulia Semeghini, Markus Greiner, Vladan Vuletić & Mikhail D, Lukin <sup>OS</sup>
vrticle	References	Citing A	articles (112)	Supplementa	al Material	PDF	HTML	Nature 622, 268–272 (2023) Cite this article
								35k Accesses   95 Citations   194 Altmetric   Metrics
ABSTRACT High-quality two-qubit gate operations are crucial for scalable quantum information proce the gate fidelity is compromised when the system becomes more integrated. Therefore, a rate, easy-to-scale two-qubit gate scheme is highly desirable. Here, we experimentally de new two-qubit gate scheme that exploits fixed-frequency qubits and a tunable ocupier in superconduction quantum incruit.								Abstract
								The ability to perform entangling quantum operations with low error rates in a scalable
								fashion is a central element of useful quantum information processing <sup>1</sup> . Neutral-atom arrays
	and si	mplifies calibra	tion procedures,	yet produces a	controlled-Z	gate in 30 ns	with a hig	have recently emerged as a promising quantum computing platform, featuring coherent
99.5%, derived from the interleaved randomized benchmarking method. Error analysis sh gate errors are mostly coherence limited. Our demonstration paves the way for large-scale								control over hundreds of qubits <sup>22</sup> and any-to-any gate connectivity in a flexible, dynamically
	impler	nentation of hig	gh-fidelity quantu	im operations.				



## Quantum systems get new operation capabilities

Demo	Demonstrating a Continuous Set of Two-Qubit Gates for Near-Term											
Quan	Quantum Algorithms											
B. Foxen	B. Foxen <i>et al.</i> (Google Al Quantum)											
Phys. Re	Phys. Rev. Lett. <b>125</b> , 120504 – Published 15 September 2020											
Article	References	Citing Articles (164)	Supplemental Material	PDF	HTML Export Cita							
ABSTRACT Quantum algorithms offer a dramatic speedup for computational problems in material science and chemistry. However, any near-term realizations of these algorithms will need to be optimized to fit within the finite resources offered by existing noisy hardware. Here, taking advantage of the adjustat coupling of groin qubits, we demonstrate a continuous two-qubit gate set that can provide a threef reduction in circuit depth as compared to a standard decomposition. We implement two gate familie an imaginary swap-like (ISWAP-like) gate to attain an arbitrary swap angle, <i>θ</i> , and a controlled-phase gate that generates an arbitrary conditional phase, <i>4</i> . Using one of each of these gates, we can perform an arbitrary two-qubit gate within the excitation-preserving subspace allowing for a complet implementation of the so-called Fermionic simulation (fitsing gate set. We benchmark the fidelity) across the entire (Sim, <i>θ</i> , <i>φ</i> ) parameter space, achieving a purity-limited average two-qubit Pauli error of 3.8 w, 10 <sup>-2</sup> ner (Sim gate												

### High-fidelity qutrit entangling gates for superconducting circuits

<u>Noah Goss</u> ⊠, <u>Alexis Morvan</u>, <u>Brian Marinelli</u>, <u>Bradley K. Mitchell</u>, <u>Long B. Nguyen</u>, <u>Ravi K. Naik</u>, <u>Larry</u> Chen, Christian Jünger, John Mark Kreikebaum, David I. Santiago, Joel J. Wallman & Irfan Siddigi

Nature Communications 13, Article number: 7481 (2022) Cite this article

9449 Accesses 48 Altmetric Metrics







# Number of qubits in quantum systems is growing

QUANTINUUM Products & Solutions Research Company News

Quantinuum Launches Industry-First, Trapped-Ion 56-Qubit Quantum Computer, Breaking Key Benchmark Record



IBM also unveiled IBM Quantum System Two, the company's first modular quantum computer and cornerstone of IBM's quantum-centric supercomputing architecture. The first IBM Quantum System Two, located in Yorktown Heights, New York, has begun operations with three IBM Heron processors and supporting control electronics.



Quantum startup Atom Computing first to exceed 1,000 qubits

Systems to be available in 2024, on path to fault-tolerant quantum computing this decade

October 24, 2023 - Boulder, CO - Atom Computing announced it has created a 1,225-site atomic array, currently populated with 1,180 qubits, in its next-generation quantum computing platform.

### Challenging our ability to simulate and validate



### Sprawling quantum industry with great job opportunities





# Quantum Systems Accelerator is solving big challenges with integrated teams

QSA integrates researchers with complementary skills from six institutions to create useful quantum systems based on neutral atoms





## Challenges to achieving useful quantum computers

Almost enough good qubits for specialized quantum use

Coherence - available compute time - very short (10s-100s of ops), driven by noise and errors

Advances in algorithms, software tools and compilers are needed to make quantum computing broadly approachable

### **Designing better qubits is hard**



# Moving towards quantum advantage for science

### Hardware technology

# Scientific algorithms and software



- Increasing qubit count
- Increasing lifetimes
- Increasing fidelity and reducing errors

- Reducing qubit count
- Decreasing operation counts
- Incorporating error resiliency

### Mathematics is needed everywhere!!!



### Applied mathematics critical across the quantum stack









Developing Novel Algorithms and Software to Advance Science with Quantum Programming Tools and Control Protocols to Harness the Power of Quantum Computers Designing and Building Prototype Quantum Processors, Controls, and Sensors Building Prototype Quantum Network and Quantum Computing Testbeds



# Designing chips and control systems with AMR and electromagnetics solvers



Image of ENCHILADA ion trap

Manuscript on arXiv:2403.00208 (2024)





### **Optimization challenges are everywhere**



$$H = \sum_{i\alpha} g_i^{\alpha} \langle \sigma_{\alpha}^i \rangle + \frac{1}{2} \sum_{ij\alpha\beta} g_{ij}^{\alpha\beta} \langle \sigma_{\alpha}^i \sigma_{\beta}^j \rangle + \cdots$$

### Only prepare and measure, do the rest classically



#### Home / Proceedings / QCE / QCE 2022

2022 IEEE International Conference on Quantum Computing and Engineering (QCE)

Accelerating Noisy VQE Optimization with Gaussian Processes

Year: 2022, Pages: 215-225 DOI Bookmark: 10.1109/QCE53715.2022.00041

#### Authors

Juliane Muller, Lawrence Berkeley National Laboratory,Computing Sciences Area,Berkeley,CA,USA Wim Lavrijsen, Lawrence Berkeley National Laboratory,Computing Sciences Area,Berkeley,CA,USA Costin Iancu, Lawrence Berkeley National Laboratory,Computing Sciences Area,Berkeley,CA,USA Wibe de Jong, Lawrence Berkeley National Laboratory,Computing Sciences Area,Berkeley,CA,USA



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### https://scikit-quant.readthedocs.io

# **Compiling...General Synthesis Problem**

Unitary



Quantum Compilation: Given unitary U, find decomposition in terms of gates G from a (universal) fixed gate set



Circuit



https://bqskit.lbl.gov

Enables:

- Algorithm discovery
- Gate set and hardware exploration
- Global circuit optimization





## Many opportunities to improve **noisy** optimization





Chadwick, Chong, QCE23, doi:10.1109/QCE57702.2023.00145



### Quantum algorithms rely on applied mathematics



Special care needs to be taken in general eigensolver due to noise in data!

HC = SCE



Urbanek, Van Beeumen, et al., J. Chem. Theory Comput. 16, 5425 (2020)

## FABLE: Fast Approximate BLock-Encodings

### Circuit synthesis tool for block encoded operators

Block encoding:

$$U = \begin{bmatrix} A & * \\ * & * \end{bmatrix}$$

- **Non-unitary** evolution on a quantum computer: Quantum linear systems, dynamic simulation, ground states, quantum thermodynamics, open quantum systems,
- FABLE circuits are:

easy to generate directly in CX, Ry and H gates efficiently compressible



### Gate complexities for 1D and 2D Laplacian





Camps, Van Beeumen, QCE22 - DOI:10.1109/QCE53715.2022.00029

### Building on Quantum Subspace Expansion: Real-time evolution for eigenvalue extraction

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Real time evolution to generate a basis of expansion states:  $|\Phi_{j,0}\rangle = e^{-iHt_j} |\Psi_0\rangle$ 



Possible to extract eigenstates by the cancellation of phases of components of the initial vector.

Promising because unlike imaginary, real time evolution is native to quantum computing.

Klymko, de Jong, Tubman et al., PRX Quantum 3 (2022)

### Building on quantum subspace expansion to extract excited states: Variational Quantum Phase Estimation (VQPE)

Original generalized eigenvalue equation:

Unitary form:

$$H\mathbf{c} = ES\mathbf{c} \longrightarrow U(\Delta t)\mathbf{c} = e^{-iE\Delta t}S$$
$$U(\Delta t)_{j,k} = \langle \Psi_0 | e^{-iH(\Delta t + t_k - t_j)} | \Psi_0 \rangle = S_{j,k+1} = S_{j-1,k}$$

Autocorrelation Function

Toeplitz structure!

Toeplitz structure means that we only need a *linear* number of measurements instead of quadratic

Approach allows extraction of the maximal number of excited states!



: T A +



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Klymko, de Jong, Tubman et al., PRX Quantum 3 (2022)

## Noise in quantum systems is the biggest nemesis



# <u>Any</u> interaction between the qubits and their environment leads to information loss



## Useful quantum science through error correction



Encode the information in multiple qubits with nonlocal correlations



## New error correction codes are being developed

Surface code

Bravyi et al., npj Quant. Inf. 4, 55 (2018)

**Heavy-Hexagon** 



Chamberland et al., Phys. Rev. X 10, 011022 (2020)

### Full error correction (hardware or software) a long-term solution, driven by increases in qubit counts and increases in fidelity



## Simple error detection and mitigation works



### 2 logical qubit H, molecule on 6 qubits with minimal basis



Urbanek et al, Phys. Rev. A 102, 022427 (2020)

## First demonstrations of error correction in 2024

#### Demonstration of quantum computation and error correction with a tesseract code

Ben W. Reichardt,<sup>1</sup> David Aasen,<sup>1</sup> Rui Chao,<sup>1</sup> Alex Chernoguzov,<sup>2</sup> Wim van Dam,<sup>1</sup> John P. Gaebler,<sup>2</sup> Dan Gresh,<sup>2</sup> Dominic Lucchetti,<sup>2</sup> Michael Mills,<sup>2</sup> Steven A. Moses,<sup>2</sup> Brian Neyenhuis,<sup>2</sup> Adam Paetznick,<sup>1</sup> Andres Paz,<sup>1</sup> Peter E. Siegfried,<sup>2</sup> Marcus P. da Silva,<sup>1</sup> Krysta M. Svore,<sup>1</sup> Zhenghan Wang,<sup>1</sup> and Matt Zanner<sup>1</sup>

#### <sup>1</sup>Microsoft Azure Quantum <sup>2</sup>Quantinuum

A critical milestone for quantum computers is to demonstrate fault-tolerant computation that outperforms computation on physical qubits. The tesseract subsystem color code protects four logical qubits in 16 physical qubits, to distance four. Using the tesseract code on Quantinuum's trapped-ion quantum computers, we prepare high-fidelity encoded graph states on up to 12 logical qubits, beneficially combining for the first time fault-tolerant error correction and computation. We also protect encoded states through up to five rounds of error correction. Using performant quantum software and hardware together allows moderate-depth logical quantum circuits to have an order of magnitude less error than the equivalent unencoded circuits.

#### Article Open access Published: 27 March 2024

### High-threshold and low-overhead fault-tolerant quantum memory

Sergey Bravyi, Andrew W. Cross, Jay M. Gambetta, Dmitri Maslov 🖾, Patrick Rall & Theodore J. Yoder

Nature 627, 778-782 (2024) Cite this article

36k Accesses | 31 Citations | 342 Altmetric | Metrics

#### Abstract

The accumulation of physical errors<sup>12,3,2</sup> prevents the execution of large-scale algorithms in current quantum computers. Quantum error correction<sup>4</sup> promises a solution by encoding *k* logical qubits onto a larger number *n* of physical qubits, such that the physical errors are suppressed enough to allow running a desired computation with tolerable fidelity. Quantum error correction becomes practically realizable once the physical error rate is below a threshold value that depends on the choice of quantum code, syndrome measurement circuit and decoding algorithm<sup>5</sup>. We present an end-to-end quantum error correction protocol that implements fault-tolerant memory on the basis of a family of low-density parity-check codes<sup>6</sup>. Our approach achieves an error threshold of 0.7% for the standard circuit-based noise

Article Open access Published: 06 December 2023

### Logical quantum processor based on reconfigurable atom arrays

Dolev Bluvstein, Simon J. Evered, Alexandra A. Geim, Sophie H. Li, Hengyun Zhou, Tom Manovitz, Sepehr Ebadi, Madelyn Cain, Marcin Kalinowski, Dominik Hangleiter, J. Pablo Bonilla Ataides, Nishad Maskara, Iris Cong, Xun Gao, Pedro Sales Rodriguez, Thomas Karolyshyn, Giulia Semeghini, Michael J. Gullans, Markus Greiner, Vladan Vuletić & Mikhail D. Lukin

Nature 626, 58-65 (2024) Cite this article

121k Accesses | 122 Citations | 958 Altmetric | Metrics

#### Quantum error correction below the surface code threshold

Google Quantum AI and Collaborators (Dated: August 27, 2024)

Quantum error correction [1–4] provides a path to reach practical quantum computing by combining multiple physical qubits into a logical qubit, where the logical error rate is suppressed exponentially as more qubits are added. However, this exponential suppression only occurs if the physical error rate is below a critical threshold. In this work, we present two surface code memories operating below this threshold: a distance-7 code and a distance-5 code integrated with a real-time decoder. The logical error rate of our larger quantum memory is suppressed by a factor of  $\Lambda=2.14\pm0.02$  when increasing the code distance by two, culminating in a 101-qubit distance-7 code with  $0.143\%\pm0.003\%$  error per cycle of error correction. This logical memory is also beyond break-even, exceeding its best physical qubit's lifetime by a factor of  $2.4\pm0.3$ . We maintain below-threshold performance when decoding in real time, achieving an average decoder latency of 63 us at distance-5 up to a million cycles, with a cycle time of  $1.1\,\mu$ s. To probe the limits of our error-correction performance, we run repetition codes up to distance-29 and find that logical performance is limited by rare correlated error events occurring approximately once every hour, or  $3\times10^9$  cycles. Our results present device performance that, if scaled, could realize the operational requirements of large scale fault-tolerant quantum algorithms.



### Understanding quantum computers through validation

# Approach enables verification, by efficiently quantifying how accurately a given computer can implement a given algorithm's quantum circuits



Uses three classes of "mirror circuits" whose success rates can be efficiently measured



Proctor et al., arXiv:2204.07568









### Solving problems beyond the reach of current hardware



#### CutQC: Using Small Quantum Computers for Large Quantum Circuit Evaluations



ASPLOS 21 - arXiv:2012.02333



# Divide-and-conquer, where the cost of stitching the problem back together depends on sparsity



### Race to the moon delivered many ancillary technologies

Quantum-inspired algorithms speedup classical computing

Novel quantum hardware technologies find way into classical computing hardware

Better understanding of quantum physics to lead to advances in classical computing



CMOS sensor, using integrated circuits....

Race for a universal quantum computer is already showing impacts beyond quantum computing



# I hope I convinced you that...

# Quantum is not scary

# And math is important for quantum

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